Modeling swarms: from micro to macro

Mirosław Lachowicz, University of Warsaw; Institute of Applied Mathematics and Mechanics

lachowic@mimuw.edu.pl

Keywords: Swarms, Integro-differential equations.

A general class of mathematical structures (integro-differential equations) that can model self-organization at the so-called mesoscopic level is proposed. The equations are of kinetic type and the interactions have nonlinear nature and may be referred to as the mesoscopic scale of description. The structures lead to interesting mathematical problems of blow-up of solutions [2], [3]) that are directly related to swarming behavior. Both microscopic and macroscopic levels are also studied ([4]).

References

- J. Banasiak, M. Lachowicz, Methods of small parameter in mathematical biology, Birkhäuser, Boston 2014.
- [2] M. Lachowicz, H. Leszczyński, M. Parisot, A simple kinetic equation of swarm formation: blow-up and global existence, Appl. Math. Letters, 57, 2016, 104–107.
- [3] M. Lachowicz, H. Leszczyński, M. Parisot, Blow-up and global existence for a kinetic equation of swarm formation, Math. Models Methods Appl. Sci., to appear.
- [4] M. Parisot, M. Lachowicz, A kinetic model for the formation of swarms with nonlinear interactions, Kinetic Related Models, 9 1, 131–164, 2016.